## CHAPTER: GRAPH THEORY

(1) Define with example: graph, nodes and edges.
(2) Define with example: directed graph, undirected graph, mixed graph, multi graph, simple graph, weighted graph and null graph.
(3) Define with example: isomorphism of graphs.
(4) Define with example: degree of a node, odd node, even node, pendant node and isolated node for undirected graph.
(5) Define with example: indegree, outdegree and total degree for directed graph.
(6) Check whether the following pair of graphs G \& H are isomorphic or not with description.
(A).

(B)


G


H
(7) Define with example: indegree, outdegree and total degree for directed graph.
(8) Define with example: indegree, outdegree and total degree for directed graph.

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| $(9)$ | Determine the number of edges in a graph with 6 nodes, 2 of degree 4 and 4 of <br> degree 2. Draw two such graphs. |
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| $(10)$ | Find whether $\mathrm{K}_{6}$ and $\mathrm{K}_{3,3}$ graphs are isomorphic or not? |
| $(11)$ | Draw a graph which contains an Eulerian circuit. |
| $(12)$ | Draw a graph which contains an Eulerian path but does not contain an Eulerian <br> circuit. |
| $(13)$ | Find under what condition $\mathrm{K}_{\mathrm{m}, \mathrm{n}}$ the complete bipartite graph will have an <br> Eulerian circuit. |
| $(14)$ | Hamiltonian circuit exists in complete bipartite graph. Justify your answer. |
| $(15)$ | Find Hamiltonian path and a Hamiltonian circuit in $\mathrm{K}_{4,3}$. |
|  | CHAPTER:TREES |
| $(16)$ | Define withexample: acyclic graph, tree, directed tree, forest, root, leaf node, <br> branch node and level of a node. |
| $(17)$ | Define with example: binary tree, complete binary tree, m-ary tree and <br> complete m- ary tree. |
| $(18)$ | Which trees are complete bipartite graphs? |
| $(19)$ | How many internal vertices does a full binary tree with h levels have? |
| $(20)$ | What is total number of nodes in a full binary tree with 20 leaves? |



| CHAPTER: RELATION AND PARTIAL ORDERING |  |
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| (1) | $A=\{1,2,3,4\}$ and $\mathrm{B}=\{1,4,6,8,9\}$ aRb iff $\mathrm{b}=\mathrm{a}^{2}$ then find relation matrix $\mathrm{M}_{\mathrm{R}}$. |
| (2) | $A=\{1,2,3,4,6\}=B, \mathrm{aRb}$ iff $\mathrm{a} / \mathrm{b}$ (a divides b ) then find relation matrix $\mathrm{M}_{\mathrm{R}}$. |
| (3) | $A=\{1,2,3,4,8\}, \mathrm{aRb}$ iff $\mathrm{a} / \mathrm{b}$ (a divides b ) then find the diagraph of relation. |
| (4) | Define the following terms with example: <br> Binary relation, Domain, Range, Reflexive, Symmetric, Transitive relation. |
| (5) | Give example of a relation which is (a) neither reflexive nor irreflexive, (b) both symmetric and antisymmetric. |
| (6) | Show whether the following relation are transitive: $\mathrm{R}_{1}=\{(1,1)\}, \mathrm{R}_{2}=\{(1,2),(2,2)\}$ $\mathrm{R}_{2}=\{(1,2),(2,3),(1,3),(2,1)\}$. |
| (7) | Let $\mathrm{X}=\{1,2,3,4\}$ and $\mathrm{R}=\{(x, y): x>y\}$. Draw the graph of R and give its matrix. |
| (8) | Define with examples: Partition, Equivalence relation, Equivalence class, Transitive closure. |
| (9) | Let $\mathrm{X}=\{1,2,3,4,5,6,7\}$ and $\mathrm{R}=\{(x, y) ; x-y$ is divisible by 3$\}$. Show that R is an equivalence relation. Draw the graph of R . |
| (10) | Let $\mathrm{X}=\{1,2,3,4,5,6,7\}$ and $\mathrm{R}=\{(x, y) ; x-y$ is even $\}$. Show that R is an equivalence relation. |
| (11) | Define with examples: Partial ordered relation, Partial ordered set, Totally ordered set. |
| (12) | If A is the set of all points in a plane, the relation 'at the same distance from the origin as' is an equivalence relation. |
| (13) | Find the transitive closure of R by Warshall's algorithm. where $A=\{1,2,3,4,5,6\}$ and $\mathrm{R}=\{(x-y):\|x-y\|=2\}$. |
| (14) | Give a relation which is both a partial ordered relation and equivalence relation on a set. |
| (15) | Draw the digraph for the following relation and determine whether the relation is reflexive, symmetric, transitive and antisymmetric. $A=\{1,2,3,4,5,6,7,8\}$ and let $x R y$ whenever $y$ is divisible by $x$. |
| (16) | Let R be the relation on set A . $\mathrm{A}=\{5,6,8,10,28,36,48\}$. Let $\mathrm{R}=\{(x, y) ; x$ is divisior of $y\}$. Draw the Hasse diagram. |
| (17) | Define with examples: Hasse diagram and Lattice. |
| (18) | Draw the Hasse diagram of the following sets under the partial ordering relation 'divides' and indicate those which are chains:(1) $\{2,4,12,24\}$ (2) $\{1,3,5,15,30\}$. |
| (19) | Let A be set of factor of positive integer m and relation is divisibility on A.i.e. $\mathrm{R}=\{(x, y) ; x, y \in A, x$ divides $y\}$. For $\mathrm{m}=45$ show that poset $(A, \leq)$ is lattice. Draw the Hasse diagram and give join and meet for the lattice. |
| (20) | $A=\{2,3,4,6,8,12,24,36\}$ is a Poset $(A, \leq)$. |

